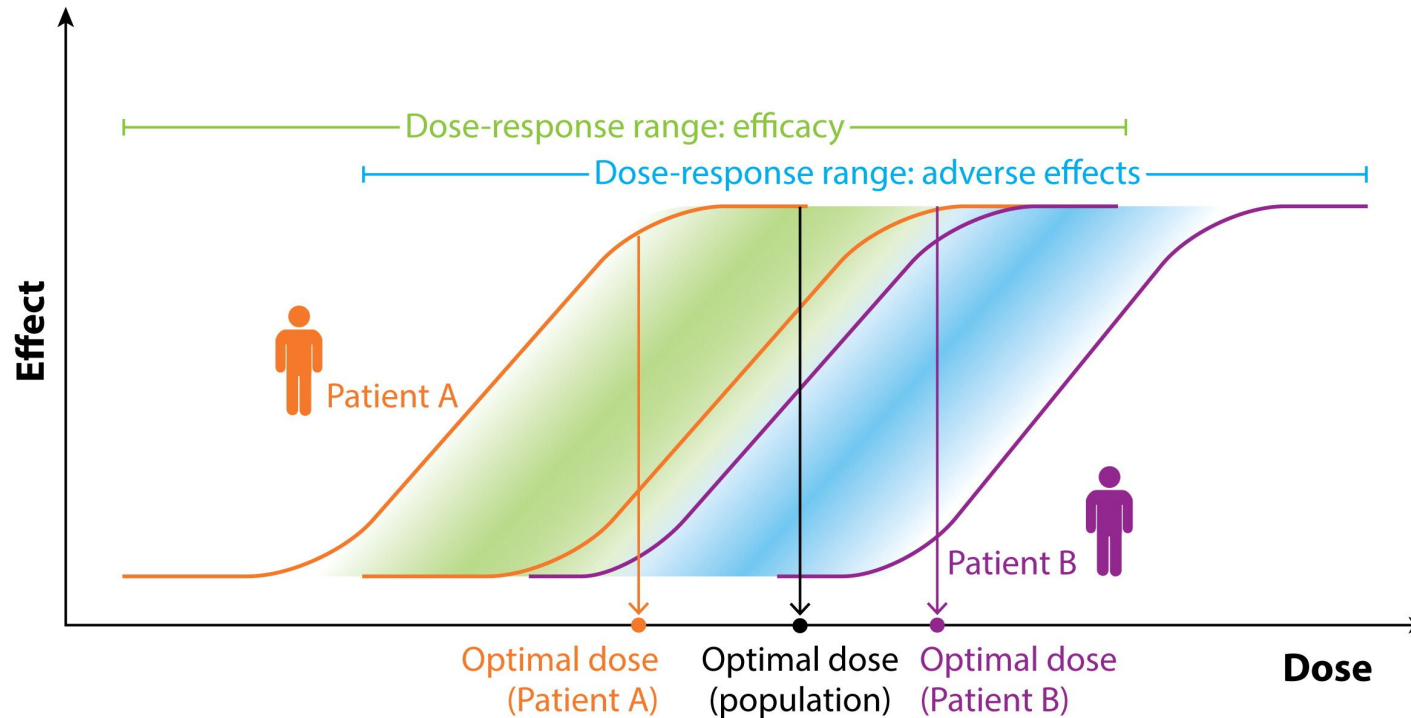


# AMIDD Lecture 9: Population Modelling and Clinical Trials



Peck, Richard W. 2018. "[Precision Medicine Is Not Just Genomics: The Right Dose for Every Patient.](#)" *Annual Review of Pharmacology and Toxicology* 58 (1): 105–22.

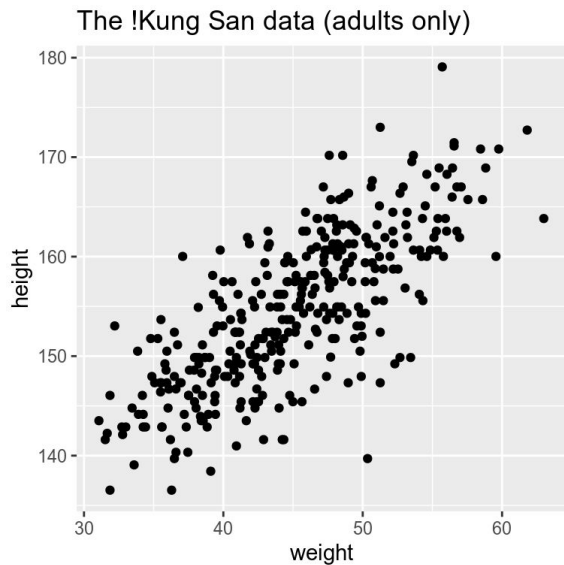
AR Peck RW. 2018.  
*Annu. Rev. Pharmacol. Toxicol.* 58:105–22

**Dr. Jitao David Zhang, Computational Biologist**

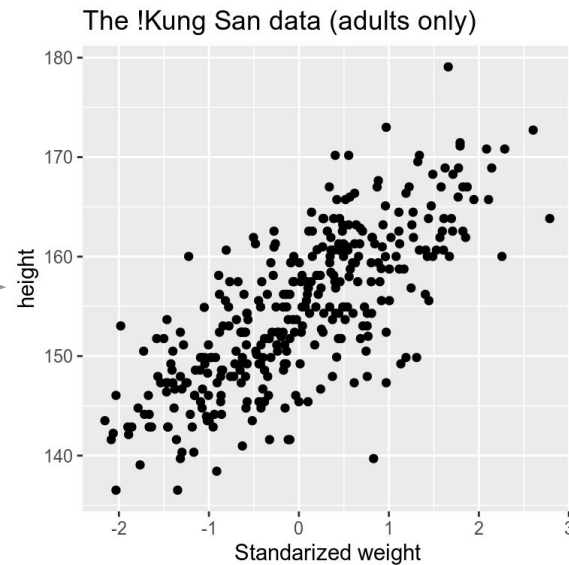
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<sup>2</sup> *Department of Mathematics and Informatics, University of Basel*

# A linear model has one level of variability



variable scaling



The Frequentist language

$$y_i = f(x) + \epsilon$$

$$f(x) = \alpha + \beta x$$

$$\epsilon \sim \mathcal{N}(0, \sigma)$$

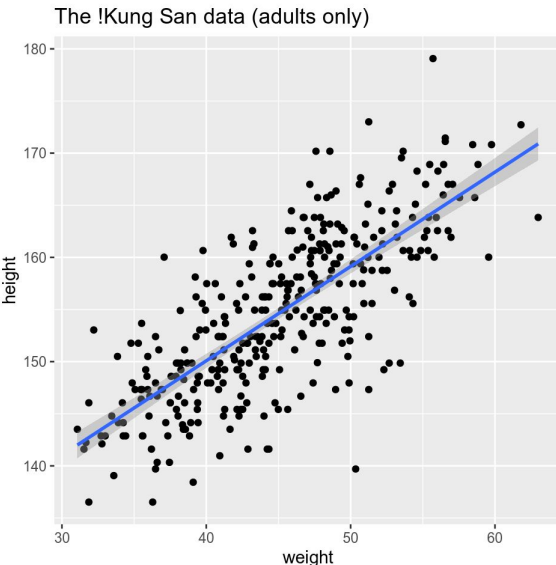
The Bayesian language,  
with some personal priors

$$y_i \sim \mathcal{N}(\mu_i, \sigma)$$

$$\mu = \alpha + \beta x_i$$

$$\alpha \sim \mathcal{N}(169, 20)$$

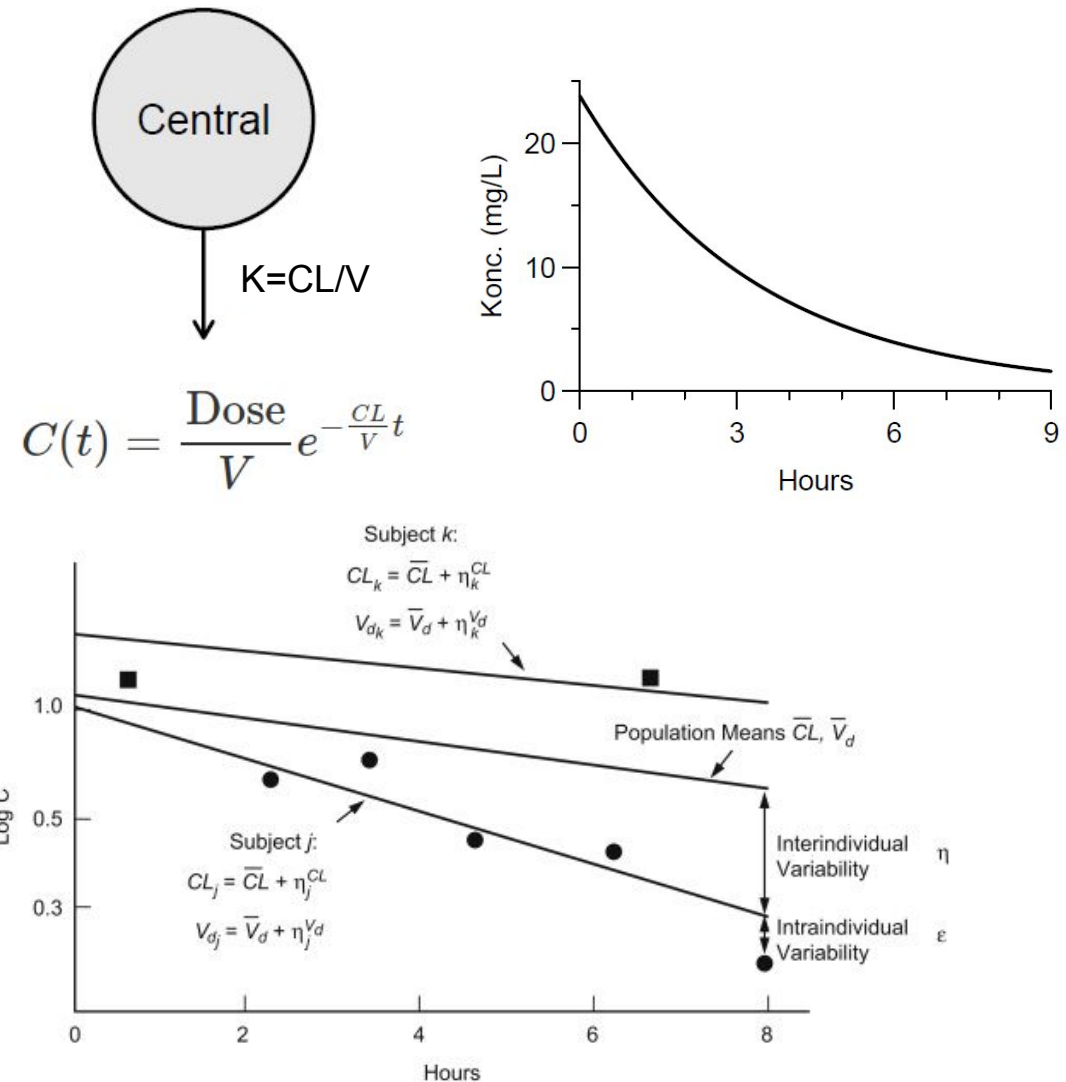
$$\sigma \sim \text{Unfoirm}(0, 50)$$



Example inspired by the *Statistical Rethinking* book by Richard McElreath

# In population modelling, we deal with two levels of variability, which calls for mixed-effect models

- Consider a simple one-compartment model, with an intravenous bolus dose (right).
- **Two types of variability**
  - **Between-subject variability**, e.g. the differences in clearance rate among patients
  - **Between-occasion variability**, e.g. the differences from one time point to the other within each patient.
- A **mixed-effect model** (mixed=fixed+random effect model, a type of hierarchical model or *multilevel model*) is needed to model such data.
- If we assume that  $V_D$  is a constant value that is the same for all subjects, but clearance varies between subjects (for instance due to ethnicity), then  $V_D$  is a fixed-effect parameter and  $CL$  is a random-effect parameter.
- If we assume that both  $V_D$  and  $CL$  vary between subjects, then both are random-effect parameters.



Bottom figure: Raymond Miller, in Principles of Clinical Pharmacology (Third Edition), 2012

# A general form of nonlinear mixed-effect models

## The Bayesian language

$$y_{ij} \sim \mathcal{N}(\mu_{ij}, \Sigma_i)$$

$$\mu_{ij} = f(t_{ij}, \beta_i, d_i)$$

$$\beta_i \sim \mathcal{N}(\beta, D)$$

- $y_{ij}$  is the  $j^{\text{th}}$  response for the  $i^{\text{th}}$  subject
- $f$  is a scalar function nonlinear with regard to  $\beta$
- $\beta$  is a  $k \times 1$  parameter vector, giving PK parameters such as absorption,  $V_D$ , and  $CL$ .
- $t_{ij}$  is the  $j^{\text{th}}$  time of measurement for the  $i^{\text{th}}$  subject
- $d_i$  is the dose of the  $i^{\text{th}}$  subject
- $j$  ranges from 1 to  $n_i$
- $D$  is a  $k \times k$  covariance matrix
- $\Sigma_i$  is an  $n_i \times n_i$  covariance matrix

## The Frequentist language

$$y_{ij} = f(t_{ij}, \underline{\beta}_i, d_i) + \varepsilon_{ij}$$

$$\underline{\beta}_i \sim N(\underline{\beta}, D)$$

$$\underline{\varepsilon}_i \sim N(\underline{0}, R_i)$$

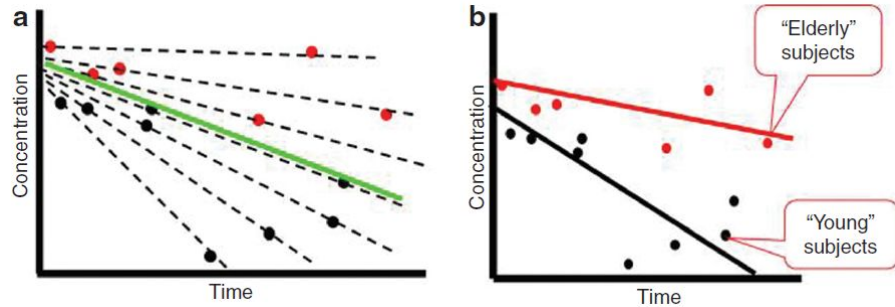
- $y_{ij}$  is the  $j^{\text{th}}$  response for the  $i^{\text{th}}$  subject
- $f$  is a scalar function nonlinear in  $\underline{\beta}$
- $\underline{\beta}$  is a  $k \times 1$  parameter vector
- $t_{ij}$  is the  $j^{\text{th}}$  time for the  $i^{\text{th}}$  subject
- $d_i$  is the  $i^{\text{th}}$  subject's dose
- $j$  ranges from 1 to  $n_i$
- $\varepsilon_{ij}$  is residual error
- $D$  is a  $k \times k$  covariance matrix
- $R_i$  is an  $n_i \times n_i$  covariance matrix

In practice, maximum-likelihood estimation (MLE) based modelling fitting is performed by numerical methods including *Laplace approximation* and *Gaussian quadrature*.

One of the mostly used software is **NONMEM** (non-linear mixed effects modeling), a commercial software. Other platforms are being actively developed, for instance GTS and ITS.

Further reading: Introduction to PK/PD Modeling for Statisticians by Alan Hartford (AbbVie), ASA Biopharm FDA-Industry Statistics Workshop. The Frequentist language was adapted from it.

# NLME modelling helps understanding clinical PK-PD parameters



Top: Mould, D R, and R N Upton. 2012. "[Basic Concepts in Population Modeling, Simulation, and Model-Based Drug Development.](#)" CPT: Pharmacometrics & Systems Pharmacology 1 (9): 1–14.

Right: Zhang, Weijiang, Dominik Heinzmann, and Joseph F. Grippo. 2017. "[Clinical Pharmacokinetics of Vemurafenib.](#)" Clinical Pharmacokinetics 56 (9): 1033–43.  $AUC_8$  and  $AUC_{168}$ : AUC from time zero to 8h or 168 h.

	Vemurafenib			
	240 mg bid	480 mg bid	720 mg bid	960 mg bid
Day 1	$n = 12$	$n = 12$	$n = 12$	$n = 16$
$AUC_8$ ( $\mu\text{g}\cdot\text{h}/\text{mL}$ )	$8.3 \pm 6.13$ (73.9)	$13.8 \pm 7.72$ (55.8)	$21.9 \pm 12.97$ (59.3)	$27.0 \pm 18.87$ (69.9)
$AUC_{24}$ ( $\mu\text{g}\cdot\text{h}/\text{mL}$ )	$40.9 \pm 23.43$ (57.3)	$62.4 \pm 35.71$ (57.2)	$111.6 \pm 34.22$ (30.7)	$130.6 \pm 71.78$ (55.0)
$C_{\max}$ 0–8 h ( $\mu\text{g}/\text{mL}$ )	$1.9 \pm 1.66$ (85.3)	$2.6 \pm 1.56$ (60.5)	$4.4 \pm 1.98$ (44.6)	$4.8 \pm 3.34$ (69.8)
$t_{\max}$ 0–8 h (h)	4.0 (1.92–8.00)	4.0 (1.95–5.00)	5.0 (2.00–8.08)	5.0 (2.00–8.00)
Day 15	$n = 10$	$n = 10$	$n = 9$	$n = 11$
$AUC_8$ ( $\mu\text{g}\cdot\text{h}/\text{mL}$ )	$117.8 \pm 50.52$ (42.9)	$233.8 \pm 106.93$ (45.7)	$343.3 \pm 151.23$ (44.1)	$392.2 \pm 126.37$ (32.2)
$AUC_{168}$ ( $\mu\text{g}\cdot\text{h}/\text{mL}$ )	$920.3 \pm 538.35$ (58.5)	$2243.5 \pm 1336.15$ (59.6)	$3127.1 \pm 1789.97$ (57.2)	$3530.3 \pm 1811.43$ (51.3)
$C_{\max}$ 0–168 h ( $\mu\text{g}/\text{mL}$ )	$17.2 \pm 7.43$ (43.1)	$35.4 \pm 17.44$ (49.2)	$52.7 \pm 22.40$ (42.5)	$61.4 \pm 22.76$ (37.1)
$t_{1/2}$ (h)	$31.5 \pm 19.05$ (60.4)	$38.4 \pm 24.18$ (63.0)	$34.9 \pm 19.48$ (55.9)	$34.1 \pm 19.66$ (57.7)
Accumulation ratio ( $AUC_8$ on day 15/day 1)	$24.9 \pm 29.4$ (118)	$23.3 \pm 16.0$ (68.7)	$18.8 \pm 12.4$ (66.0)	$23.2 \pm 16.5$ (71.1)

# Clinical studies and clinical trials

- A **clinical study** is research using human volunteers (*i.e.* participants), with the intention to add to medical knowledge.
- Two main types of clinical studies: **clinical trials** (also called interventional studies) and observational studies. In clinical trials, participants are assigned to specific **interventions** by the investigator, which is not the case in observational studies.
- **Most drug and vaccine candidates fail.**
- Only drugs undergoing successful clinical studies are approved by regulatory agencies. For instance, FDA usually requires that a drug must show statistical significance in two ‘adequate and well-controlled’ pivotal Phase III studies as a precondition of its approval.

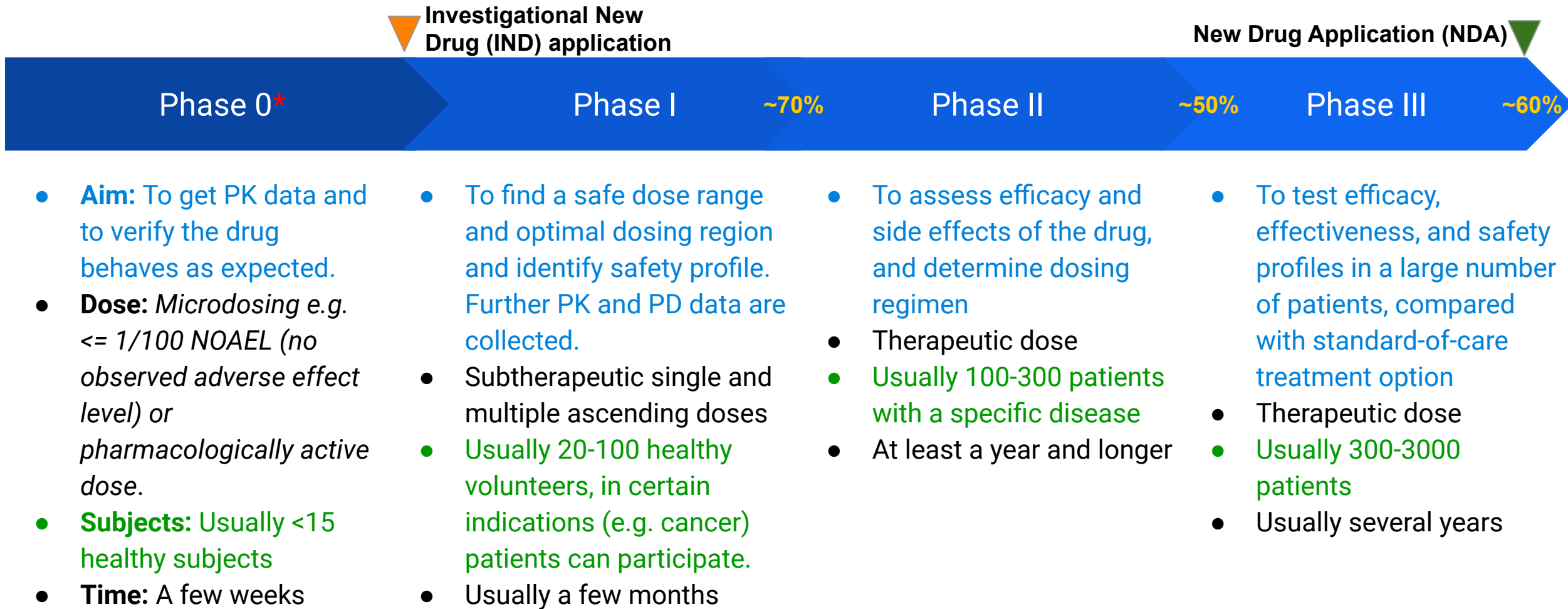
## Probability of Success<sup>2</sup> by Clinical Trial Phase and Therapeutic Area

	<i>P1 to P2</i>	<i>P2 to P3</i>	<i>P3 to Approval</i>	<i>Overall</i>
<i>Oncology</i>	57.6	32.7	35.5	3.4
<i>Metabolic/Endocrinology</i>	76.2	59.7	51.6	19.6
<i>Cardiovascular</i>	73.3	65.7	62.2	25.5
<i>Central Nervous System</i>	73.2	51.9	51.1	15.0
<i>Autoimmune/Inflammation</i>	69.8	45.7	63.7	15.1
<i>Genitourinary</i>	68.7	57.1	66.5	21.6
<i>Infectious Disease</i>	70.1	58.3	75.3	25.2
<i>Ophthalmology</i>	87.1	60.7	74.9	32.6
<i>Vaccines (Infectious Disease)</i>	76.8	58.2	85.4	33.4
<i>Overall</i>	66.4	48.6	59.0	13.8
<i>Overall (Excluding Oncology)</i>	73.0	55.7	63.6	20.9

Source: Chi Heem Wong, Kien Wei Siah, Andrew W Lo. "Estimation of clinical trial success rates and related parameters." *Biostatistics* 20(2): April 2019, Pages 273-286. Published online: 31 January 2018. DOI: 10.1093/biostatistics/kxx069

Data between 2000 and 2015 of 406,038 trials (of which 185,994 were unique) and well over 21,000 compounds were collected. The table was formatted by [ACSH](#).

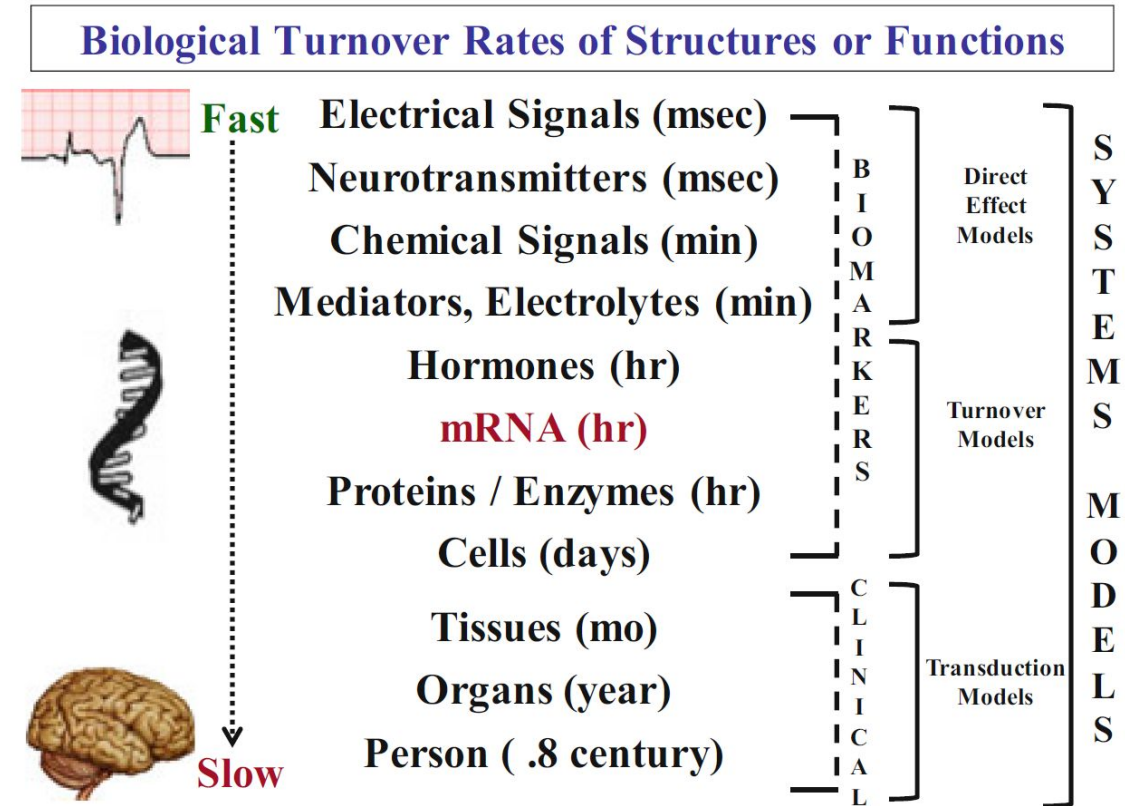
# Phases of clinical trials prior to approval



\* Since early 2000. See an update-to-date review by Burt, Tal, Graeme Young, Woojin Lee, Hiroyuki Kusuhara, Oliver Langer, Malcolm Rowland, and Yuichi Sugiyama. 2020. "[Phase 0/Microdosing Approaches: Time for Mainstream Application in Drug Development?](#)" Nature Reviews Drug Discovery 19 (11): 801–18.

# We use clinical endpoints, biomarkers, and surrogate endpoints to judge whether a drug works or not

- **Clinical endpoints:** direct evidence of clinical outcome, reflecting how a patient feels (e.g. relieve of anxiety and depression), functions (e.g. hospitalization), responds to pathogens (e.g. infection rate), or how long a patient survives (e.g. progression-free survival, overall survival). It can be expensive and take long to measure them.
- **Biomarkers:** objectively measured and evaluated as an indicator of normal biological, pathogenic processes or pharmacological response to a drug, which can take many forms
  - **Biochemical**, e.g. alanine aminotransferase (ALT), CD4+, cholesterol
  - **Anatomical/morphological**, e.g. tumor Size, artery diameter, and imaging results of PET, CT-Scan, MRI, etc.
  - **Histological**, e.g. biopsy pathology, whole blood count (WBC)
  - **Other measurements**, e.g. Blood pressure, pain relief, QT interval in electrocardiogram, etc.
- **Surrogate endpoints:** biomarkers supported by strong evidence so that they may substitute a clinical end point when obtaining registration, e.g. neutralising antibodies against spike proteins of the coronavirus in the plasma as a surrogate of reduced rate of infection.



Jusko, William J. 2016. "[Foundations of Pharmacodynamic Systems Analysis.](#)" In Systems Pharmacology and Pharmacodynamics, edited by Donald E. Mager and Holly H.C. Kimko, 161–75. AAPS Advances in the Pharmaceutical Sciences Series. Cham: Springer International Publishing.

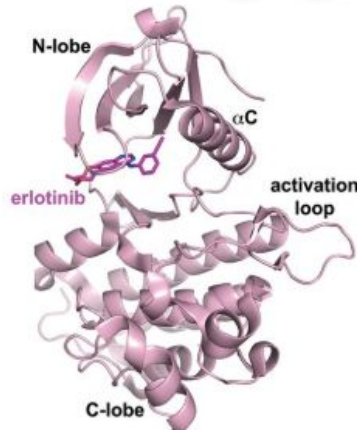


# Conclusion of the course

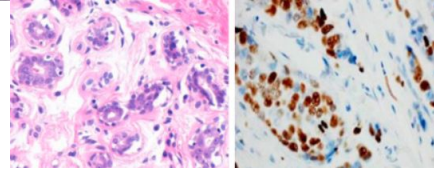
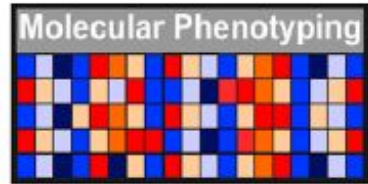
## Multiscale Modelling of Drug Mechanism and Safety

Forward translation

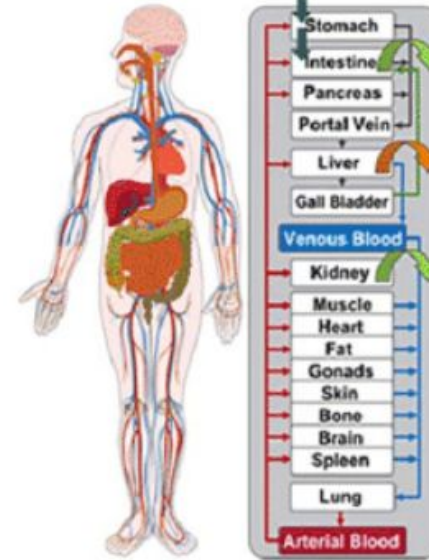
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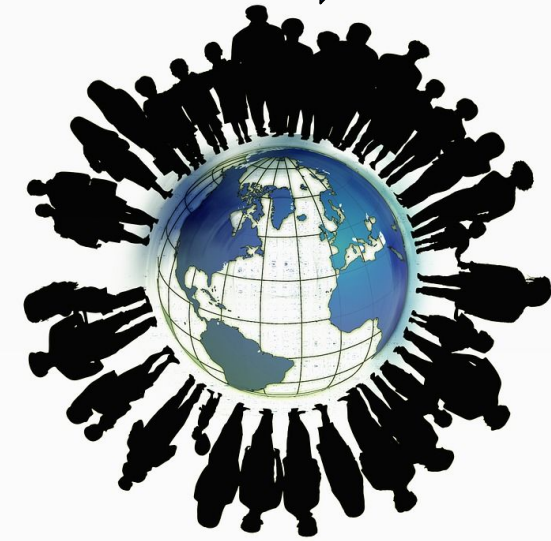
Molecular modelling



Omics & cellular modelling



Organ & system modelling



Populational modelling

Reverse translation

Principles that we covered: molecular biology (the central dogma), bioinformatics (DP and MC/HMM), chemoinformatics and CADD (molecular descriptors, QSAR, docking), omics (RNA sequencing), pharmacology (PK, PD, PBPK), population modelling (NLME), ...

# Thank you for...

- Attending the course virtually;
- Giving me and the course feedback;
- Hopping between disciplines together with me;
- Reading (maybe too) much material;
- Taking time for offline activities;
- Asking and answering questions;
- Googling strange terms that you have never heard of;
- Bearing with my accent, speaking speed, and poor drawing;
- Being interested in applied mathematics and informatics in drug discovery.

# Backup

# Increased success rate in since 2014?

